

# INVESTIGATION OF UNSTEADY TWO-PHASE FLOW OF WET STEAM THROUGH NOZZLES

*Mofreh H. Hamed*

Mechanical Power Engineering Department, Faculty of Engineering,  
Menoufia University, EGYPT

## ABSTRACT

A numerical model for the solution of unsteady one-dimensional two-phase flow of wet steam accompanied with spontaneous condensation in supersonic nozzles is described. The effect of introducing the coefficient  $\beta$ , which is a correction for nucleation work of nucleation rate, is taken into account. The effect of condensation coefficient  $\alpha_c$  is also presented. Comparisons between predictions of the suggested method and experimental results of both the present experiments and published ones and also between other theoretical works were also made there. The comparisons show satisfactory agreement.

**Keywords :** Spontaneous condensation, nucleation, supersonic nozzle, unsteady flow, and vapour subcooling.

## INTRODUCTION

Problems of multiphase flow appear recently in many areas of technology and energy production. Two-phase flow of wet steam in the last stages of steam turbines, of both conventional and nuclear power plants, has been considered as one of the greatest importance of these problems. The wet steam flow, was found to be affected mainly with the so called "condensation coefficient". Condensation coefficient is defining the fraction of the impinging vapour molecules which adhere to the surface of water droplets suspended inside wet steam medium.

In view of earliest measurements of this coefficient, Sherwood and Johannes [1] obtained different values for the condensation coefficient of condensed liquids and concluded that all liquids did not have condensation coefficients equal unity. Young [2] has suggested recently that the condensation coefficient has similar values for wet steam flows under equilibrium conditions (i.e., when the condensation rate is zero), whilst it has different values when non-equilibrium condition prevails and consequently a net condensation effect occurs. Therefore, it is common to take the value of the

condensation coefficient equal unity in the most of the numerical models, which treat nucleation and condensation processes [2,3]. Gajewski *et al.* [4] have presented a theoretical approach which considers variable values for both the condensation and evaporation coefficients during non-equilibrium condensation processes of water vapour.

In simulating and solving many of the condensation problems, such as shock waves and losses, good agreement between measurements and predictions of condensation theories must be achieved. This agreement was confirmed by utilizing different values for the condensation and evaporation coefficients as in [5] and [6]. It is of great importance to note that Hill [5] and Soltanov *et al.* [6] used random values for these coefficients. At present, Mahmoud [7] revised most of the published data on the condensation and evaporation coefficients in a numerical procedure in order to conjoin these coefficients with the pressure value at Wilson point in free molecular, intermediate and continuum flow regimes. He showed that the condensation coefficient depends significantly upon the pressure at Wilson point, vapour subcooling,

droplet size, evaporation coefficient and index of isentropic expansion.

The present work verifies a theoretical model, based on one dimensional, unsteady two-phase flow approximations, to simulate the spontaneous condensation during steam expansion through supersonic nozzles. The proposed model utilizes the suggested formulation of the condensation coefficient in Reference 7 and selected values for the coefficient  $\beta$ , in the nucleation rate equation, to acquire satisfactory agreement between pressure measurements, from literature or present experiments through nucleation and condensation zones, and present predictions. Furthermore, a detailed analysis for the effect of both the condensation coefficient  $\alpha_c$  and correction coefficient  $\beta$  on the condensation characteristics, such as nucleation rate, vapour subcooling and droplet size are also enclosed in the present work.

**THEORETICAL TREATMENT**

**Phase Description and Phase Transformation**

The general characteristics of adiabatic, spontaneous condensation, unsteady one-dimensional steam flow through supersonic nozzles are described below under the following assumptions:

- i- Vapour density is low enough, so that it is considered thermally perfect.
- ii- Water-phase consists of monodispersed incompressible spherical droplets.
- iii- Initial flow condition corresponds to the single-phase condition or wet steam condition.
- iv- Mechanism of water-phase formation is generally the spontaneous formation (i.e., homogeneous nucleation) of water nuclei from the pure vapour at sufficiently high supersaturation.
- v- Water droplet is so small enough, that the vapour and water phases are in dynamic equilibrium.
- vi- The initial flow properties of steam may be expressed as follows [8]:

$$T_s = 273 + 10 \times \left(\frac{p}{9.81}\right)^{1/4}$$

$$\sigma = 0.132 - 0.207 \times 0.001 \times T_s$$

$$\zeta = (762.4 - 0.6 \times T_s) \times 4.19$$

**Flow Equations**

With the above assumptions, a set of unsteady equations governing the mass, momentum and energy transfer in the steam flow along the flow element shown in Figure 1 are presented below. The basic equations were illustrated previously by Danelen [8]. Continuity equation of vapour phase:

$$\frac{\partial \rho_1 A}{\partial t} + \frac{\partial \rho_1 c A}{\partial z} = -\gamma \cdot A \tag{1}$$

Momentum equation for vapour phase

$$\frac{\partial \rho_1 c A}{\partial t} + \frac{\partial (\rho_1 c^2 + p) \cdot A}{\partial z} = -c \cdot \gamma \cdot A + p \frac{\partial A}{\partial z} \tag{2}$$

The unsteady equation for the energy conservation of the vapour phase contained in the flow element of Figure 1 is expressed by:

$$\rho_1 \frac{\partial i_{o1}}{\partial t} + \rho_1 c \frac{\partial i_{o1}}{\partial z} = \frac{\partial p}{\partial t} + \gamma \cdot (i_1 - \mu_f) \tag{3}$$

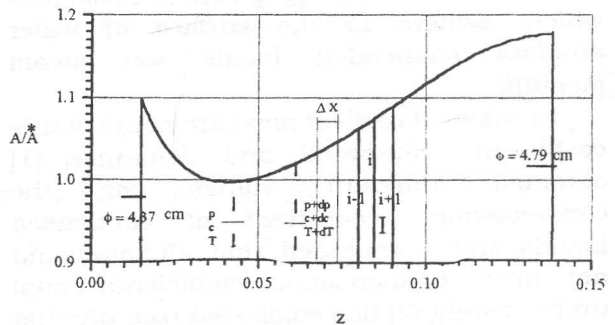


Figure 1 Profile of nozzle and flow element.

Here,  $i_{o1}$  is the stagnation enthalpy of the vapour phase,  $\mu_f$  is the Gibbs function of the substance undergoing phase conversions. For the case considered,  $\mu_f$  is defined as:

$$\mu_r = i_1 - T_1 \cdot S_1 \quad (4)$$

While the density distribution of condensed phase (droplet) with respect to its size in one-dimensional flow is as follows:

$$\frac{\partial \|N\| A}{\partial t} + \frac{\partial \|N\| c A}{\partial z} = -J \cdot A \quad (5)$$

$$\frac{\partial \|N\| \langle r_d \rangle A}{\partial t} + \frac{\partial \|N\| c \langle r_d \rangle A}{\partial z} = A(J \cdot r_* + a_2 \|N\|) \quad (6)$$

$$\frac{\partial \|N\| \langle r_d^2 \rangle A}{\partial t} + \frac{\partial \|N\| c \langle r_d^2 \rangle A}{\partial z} = A(J \cdot r_*^2 + 2 \cdot a_2 \|N\| \langle r_d \rangle) \quad (7)$$

Where,

$$\|N\| = \int N(r) \cdot dr \quad (8)$$

$$\langle r_d^2 \rangle = \int f(r) \cdot r^2 \cdot dr \quad (9)$$

$$f(r) = \frac{N(r)}{\|N\|} \quad (10)$$

Where,  $N(r)$  is the non-normalizing density distribution of droplet.

**Supplementary Equations**

The system of Equations 1 to 3 for the vapour phase and 5 to 7 for the condensed phase may be extended by the following equations:

a- Thermal equations of state used in Reference 12 are:

$$p_1 = \rho_1 \cdot R_B \cdot T_1, \quad \text{Where, } R_B = B \cdot R \quad (11)$$

$$i_1 = \frac{\gamma}{(\gamma - 1)} \cdot \frac{p_1}{\rho_1} + \text{const.} \quad (12)$$

b- An equation for the vapour entropy is:

$$S_1 = S_{in} + \frac{R_B}{(\gamma - 1)} \ln \left[ \frac{p_1}{p_{in}} \left( \frac{\rho_{in}}{\rho_1} \right)^\gamma \right] \quad (13)$$

c- The Kelvin-Helmholtz relation, describing the radius of a critical droplet in metastable equilibrium with a supercooled vapour is:

$$r_* = \frac{2 \cdot \sigma_2 \cdot T_s}{\rho_2 \cdot \zeta \cdot \Delta T_s} \quad (14)$$

d- An equation for nucleation  $J$  is [6]:

$$J = \left( \frac{p_1}{kT_1} \right)^2 \cdot v_m \cdot \sqrt{\frac{2 \cdot \sigma_2 \cdot m_o}{\pi}} \cdot \text{Exp} \left( -\beta \frac{\Delta w(r_*)}{kT_1} \right) \quad (15)$$

Where,

$\Delta w(r_*)$  is the nucleation work and is determined as in Reference 6 by the formula:

$$\Delta w(r_*) = \frac{4}{3} \pi \cdot r_*^2 \cdot \sigma_2 \quad (16)$$

e- The rate of phase conversion (mass flux of condensed phase)  $\chi$  may be expressed as follows based on the equation of density distribution of droplet [8,9]:

$$\chi = \int N(r) \cdot \frac{dm(r)}{dt} \cdot dr \quad (17)$$

Where  $\frac{dm(r)}{dt}$  is the mass velocity change of droplet, which can be expressed by the following relation:

$$\frac{dm(r)}{dt} = \frac{4\pi r_d^2 \alpha_c}{\sqrt{2\pi R_B T_1}} \cdot \left( 1 - \sqrt{\frac{T_1}{T_2}} \right) \quad (18)$$

By inserting Equations 8, 9, 10 and 18 in Equation 17 then,

$$\chi = \bar{a} \cdot \|N\| \cdot \langle r_d^2 \rangle, \quad (19)$$

$$\text{Where, } \bar{a} = \frac{4\pi \alpha_c}{\sqrt{2\pi R_B T_1}} \cdot \left( 1 - \sqrt{\frac{T_1}{T_2}} \right)$$

**Method of solution**

With reference to the typical arrangement shown in Figure 1, the channel was divided into a number of  $\Delta x = L/n$  where,  $n$  is the number of steps.

The system of Equations 1 to 3 and also 5 to 7 can be integrated with respect to time using the finite difference technique [11], under the following conditions:

**Inlet conditions**

$$t = 0, \quad x \in [0, L],$$

$$p = p_m, \quad \rho = \rho_m \quad \text{and} \quad c = c_m$$

**Exit conditions**

$$x = L \quad \text{and} \quad p = p_2$$

**Boundary conditions**

The index  $i$  and  $i+1$  are the boundary of  $I^{th}$  cell as shown in Fig. (2). The quantities at the boundary of cell  $I$  can be calculated as follows:

$$a = \frac{1}{2} \sqrt{\gamma \cdot (p_{i-1} + p_i) \cdot (\rho_{i-1} + \rho_i)}$$

$$\tilde{p} = \frac{1}{2} [p_{i-1} + p_i \cdot a \cdot (c_{i-1} - c_i)]$$

$$u = \frac{1}{2} [c_{i-1} + c_i + \frac{(p_{i-1} - p_i)}{a}]$$

$$\rho^l = \frac{(\gamma + 1)\tilde{p} + (\gamma - 1)p_{i-1}}{(\gamma - 1)\tilde{p} + (\gamma + 1)p_{i-1}} \cdot \rho_{i-1}$$

$$\rho^r = \frac{(\gamma + 1)\tilde{p} + (\gamma - 1)p_i}{(\gamma - 1)\tilde{p} + (\gamma + 1)p_i} \cdot \rho_i$$

$$D^l = c_{i-1} - \frac{a}{\rho_{i-1}}$$

$$D^r = c_i + \frac{a}{\rho_i}$$

Under the following conditions:

**$D^l$  and  $D^r$  are both positive**

$$c_i = c_{i-1}, \quad p_i = p_{i-1} \quad \text{and} \quad \rho_i = \rho_{i-1}$$

**$D^l$  and  $D^r$  are both negative**

$$c_i = c_i, \quad p_i = p_i \quad \text{and} \quad \rho_i = \rho_i$$

**$D^l$  and  $D^r$  are negative and  $u > 0.0$**

$$c_i = u, \quad p_i = \tilde{p} \quad \text{and} \quad \rho_i = \rho^l$$

$$c_i = u, \quad p_i = \tilde{p} \quad \text{and} \quad \rho_i = \rho^r$$

The time step  $\Delta t$  is calculated from the condition:

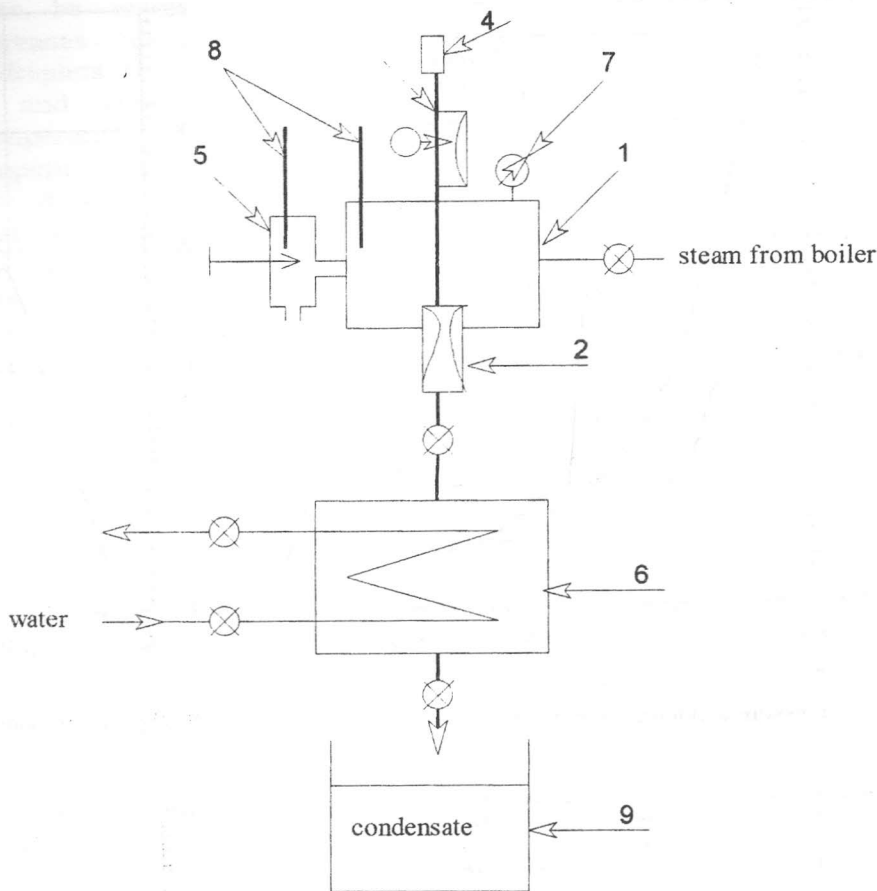
$$\Delta t < \frac{\Delta x}{q} \quad \text{where,}$$

$$q = \max. [|D^l|; |D^r|]$$

**EXPERIMENTAL APPARATUS AND MEASURING DEVICE**

A schematic diagram of the experimental set-up is shown in Figure 2. It consists of a steam vessel (1), which is fed with wet steam from a fire-tube boiler of one ton/hour capacity at a maximum pressure of 6 bar. The investigated nozzle (2) was made from brass and manufactured with the profile shown in Figure 1. The tested nozzle is screwed into the bottom of the steam vessel and is supplied with steam from this vessel. Exhaust steam is condensed in a surface condenser (6) and is rated in a metering tank.

Measurements of the static pressure distribution along the nozzle axis, steam flow rate, static vapour temperature, and the wetness fraction by the throttling calorimeter (5) at the nozzle inlet were carried out. The axial pressure variation along the nozzle axis was measured with the aid of a Stodola search tube (3) of nominal diameter of 3.31 mm. The Stodola search tube was equipped with a pressure transducer (4). The probe is traversed in increments of 2.5 mm by rotating a calibrated dial (D). The vapour velocity at the nozzle inlet was obtained by measuring the steam flow rate, vapour pressure and temperature inside the vessel. A mercury-in-glass thermometer (8) was used to obtain the static temperature of the wet steam flow in the vicinity of the nozzle inlet inside the steam vessel. Furthermore, a pressure gauge (7) was used to indicate the vessel steam pressure. The steam vessel is connected to a throttling calorimeter (5) with a mercury in glass thermometer (8) and a pressure gauge in order to identify the steam wetness ahead of nozzle entrance.



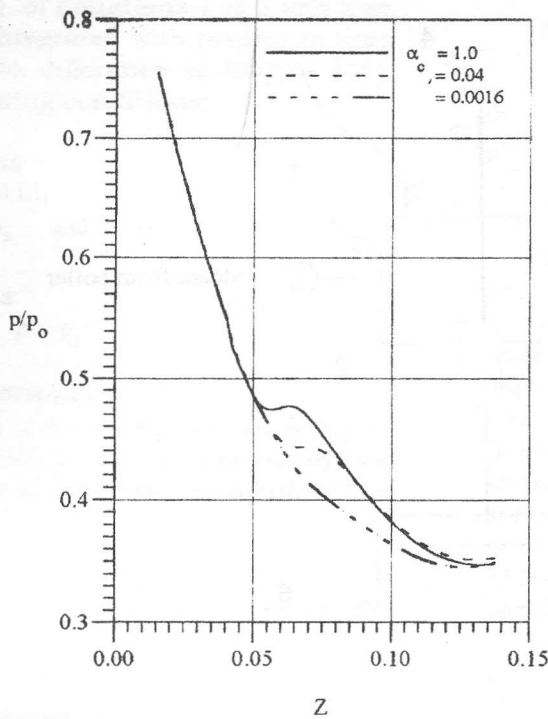
- |                        |                           |
|------------------------|---------------------------|
| 1- steam vessel        | 5- throttling calorimeter |
| 2- nozzle              | 6- surface condenser      |
| 3- search tube         | 7- pressure gauge         |
| 4- pressure transducer | 8- thermometer            |
|                        | 9- metering tank          |

Figure 2 Schematic diagram for the experimental setup

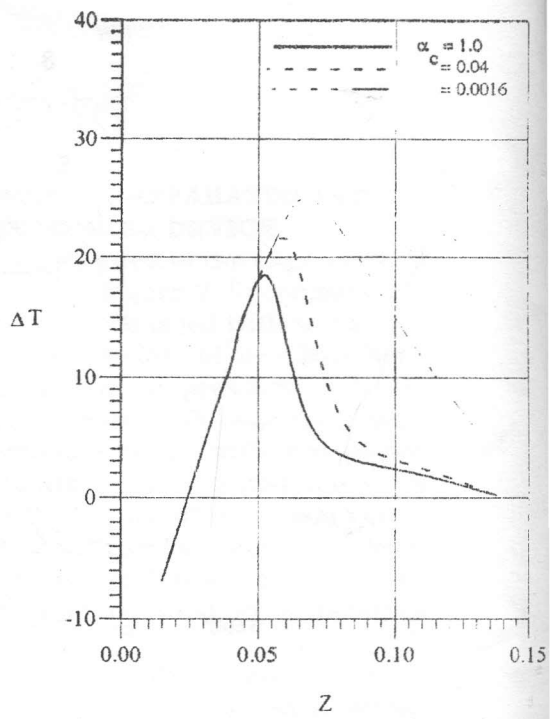
### RESULTS AND DISCUSSION

The predictions, presented herein are obtained for the nozzle profile, shown in Figure 1. These predictions illustrate the effects of changing the initial pressure, condensation coefficient  $\alpha_c$  and the coefficient  $\beta$  on the two-phase flow characteristics. The boundary conditions are stated with these predictions. Figure 3 presents the effect of changing  $\alpha_c$  on the variation of the axial pressure, vapour subcooling, phase conversion rate and mean

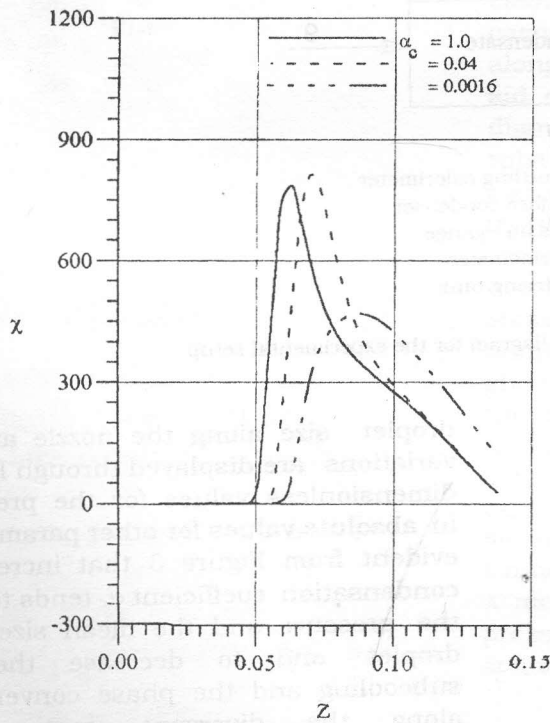
droplet size along the nozzle axis. These variations are displayed through Figure 3 in dimensionless values for the pressure and in absolute values for other parameters. It is evident from Figure 3 that increasing the condensation coefficient  $\alpha_c$  tends to increase the pressure and the mean size of water droplet and to decrease the vapour subcooling and the phase conversion rate along the divergent section of the investigated nozzle.



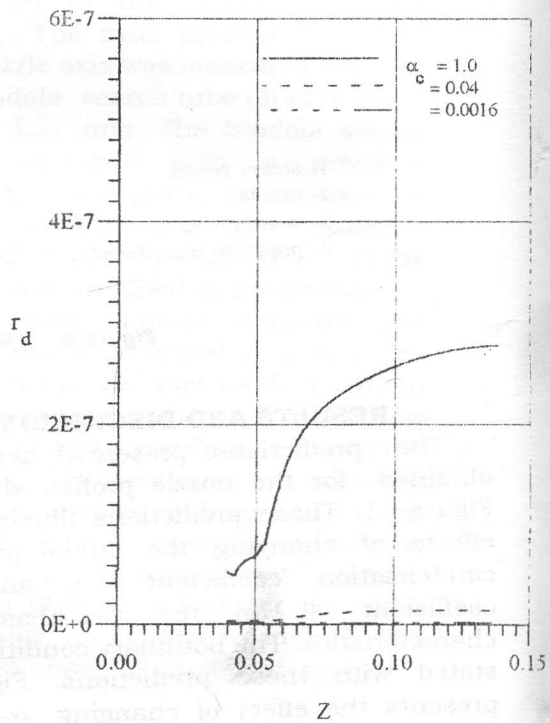
a- pressure variation along nozzle axis.



b- vapour subcooling along nozzle axis.



c- phase conversion rate along nozzle axis.



d- mean droplet size along nozzle axis.

**Figure 3** Effect of changing the condensation coefficient ( $\alpha_c$ ) on the flow characteristics at constant values of  $p_0 = 6.83$  bar,  $\beta = 1.0$  &  $\Delta T_1 = 3$  K

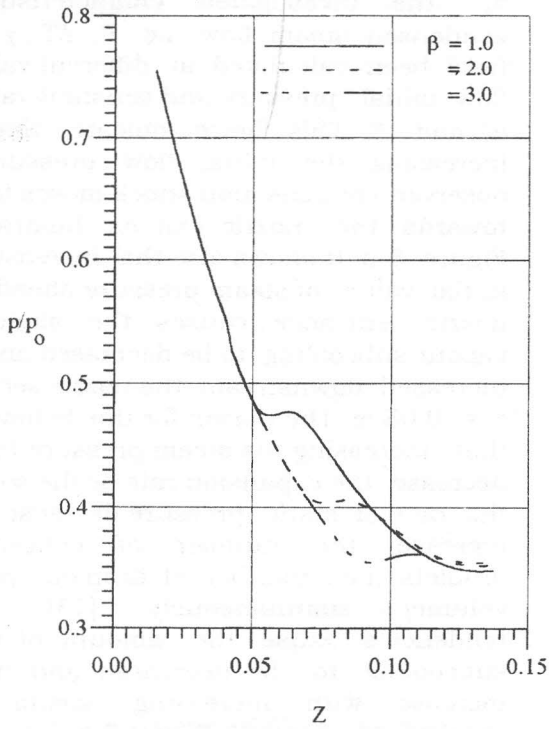


This tendency can be explained as the coefficient  $\alpha_c$  increases the rate of heat dissipation from droplets surface into the ambient vapour and consequently the vapour phase temperature are increased, and then the vapour subcooling ( $\Delta T$ ) is decreased. This dissipated rate of condensation heat is accompanied by an adverse pressure gradient or so-called "condensation shock" as shown clearly in Figure 3-a behind nozzle passage after  $z=0.05$  m. This behaviour of results was previously confirmed in the literature [5,6]. Therefore, decreasing ( $\Delta T$ ) with increasing  $\alpha_c$  is accompanied with increasing both the rate of phase conversion and droplet growth beside the occurrence of condensation shock corresponding to the location of  $\chi$  and  $r_d$  increase.

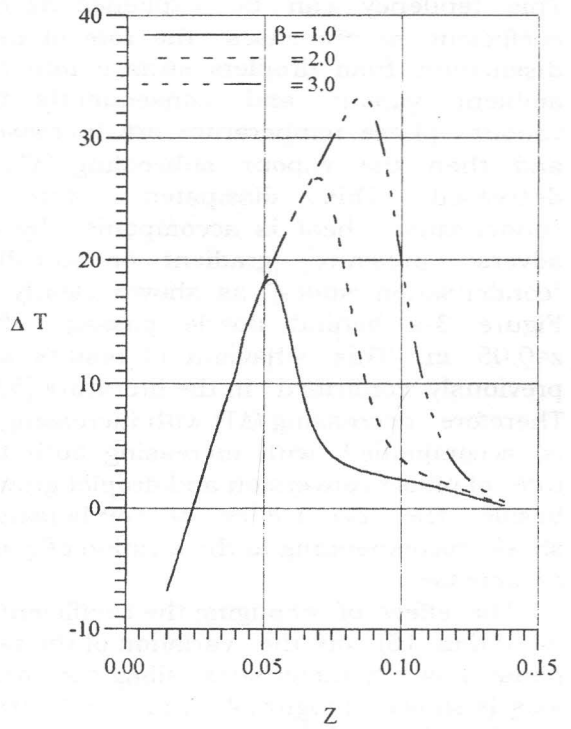
The effect of changing the coefficient  $\beta$ , (Equation 15), on the variation of the two-phase flow characteristics along the nozzle axis is shown in Figure 4. From this figure it can be observed that, increasing coefficient  $\beta$  damps the condensation shock that formed within the nozzle divergent portion, Figure 4-a and then increasing the amount of vapour subcooling, rate of phase conversion and mean droplet size, Figures 4-b, 4-c and 4-d. An explanation for this tendency is obtained using a previous conception for the variation of nucleation rate with the subcooling amount ( $\Delta T$ ) and steam pressure  $P$ . Gyarmathy [13] showed that the expression of  $J$  is generally very sensitive to the numerical parameters such as the coefficient  $\beta$ . Furthermore, he concluded that changing the nucleation rate reflects in a conjugate change on ( $\Delta T$ ). The reason for this tendency is due to the variation of material properties such as water surface tension [13]. In conclusion, as the coefficient  $\beta$  increases the nucleation rate  $J$  is decreased and therefore, the vapour subcooling, rate of phase conversion and mean bubbles size are increased. In Figure

5, the investigated characteristics of condensed steam flow; i.e.  $P$ ,  $\Delta T$ ,  $\chi$  and  $r_d$  have been calculated at different values of flow initial pressure and constant values of  $\alpha_c$  and  $\beta$ . This figure indicates that with increasing the initial flow pressure, the observed condensation shock moves forward towards the nozzle exit as illustrated in Figure 5-a. It shows also that increasing the initial value of steam pressure ahead of the nozzle entrance causes the amount of vapour subcooling to be decreased and then increased downstream the nozzle section at  $z = 0.05$  m. The reason for this behaviour is that increasing the steam pressure tends to decrease the expansion rate or the so-called the rate of static pressure decrease and to increase the number of concentrated droplets (i.e., number of droplets per unit volume) simultaneously [13]. These tendencies cause the amount of vapour subcooling to be decreased and then to increase with increasing steam initial pressure as shown in Figure 5-b. Decreasing the expansion rate, causes the vapour subcooling to decrease as predicted by equation (3.1.2) in [13], whilst increasing the number of concentrated droplets causes the vapour subcooling to increase due to increasing the rate of heat transfer between the two phases. Therefore, due to the behaviour of  $\Delta T$  variation with the three tested values of steam initial pressure and the difference between nucleation rates; the  $\Delta T$  peak can move towards the nozzle exit and then reflects the trend of  $\Delta T$  curves.

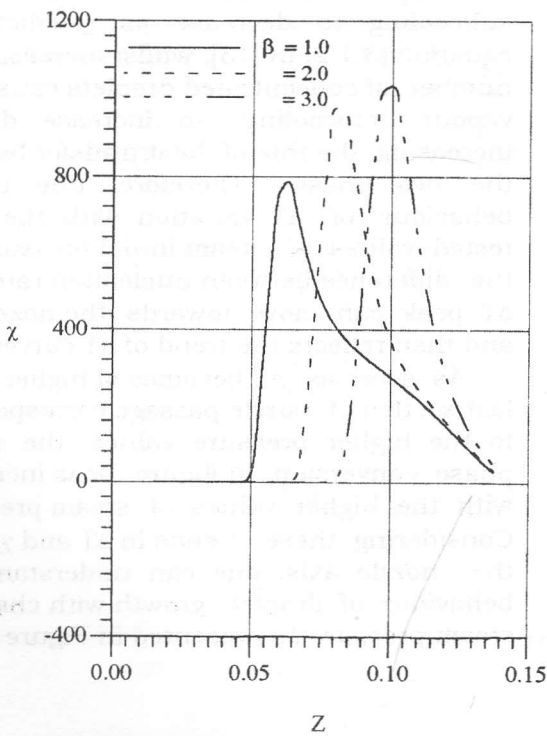
As soon as  $\Delta T$  becomes of higher in the last section of nozzle passage corresponding to the higher pressure values, the rate of phase conversion in Figure 5-c is increased with the higher values of steam pressure. Considering these trends in  $\Delta T$  and  $\chi$  along the nozzle axis, one can understand the behaviour of droplet growth with changing steam pressure as presented in Figure 5-d.



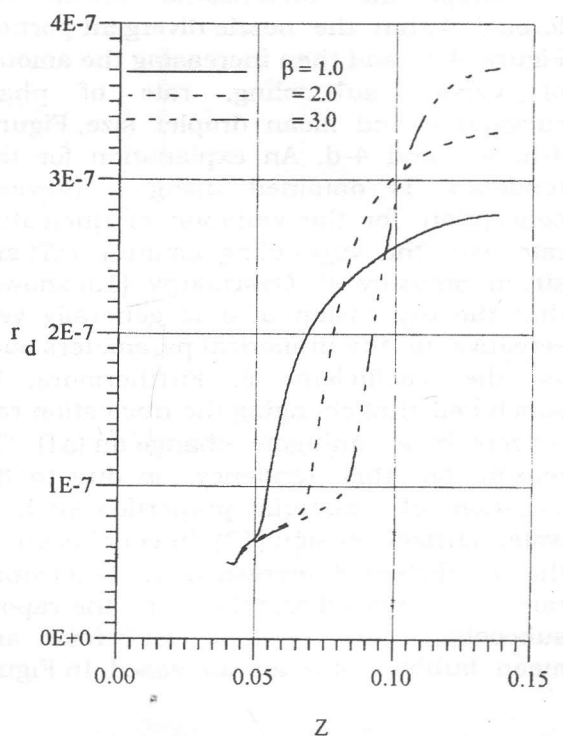
a- pressure variation along nozzle axis.



b- vapour subcooling along nozzle axis.



c- rate of phase conversion along nozzle axis.

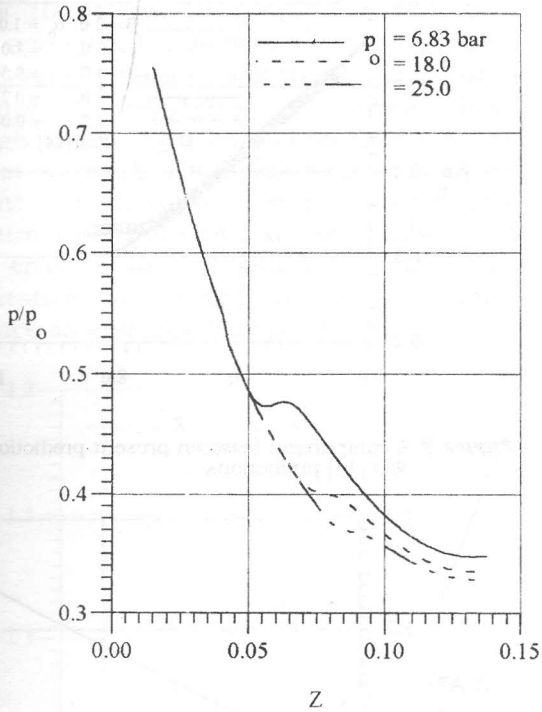


d- mean droplet size along nozzle axis.

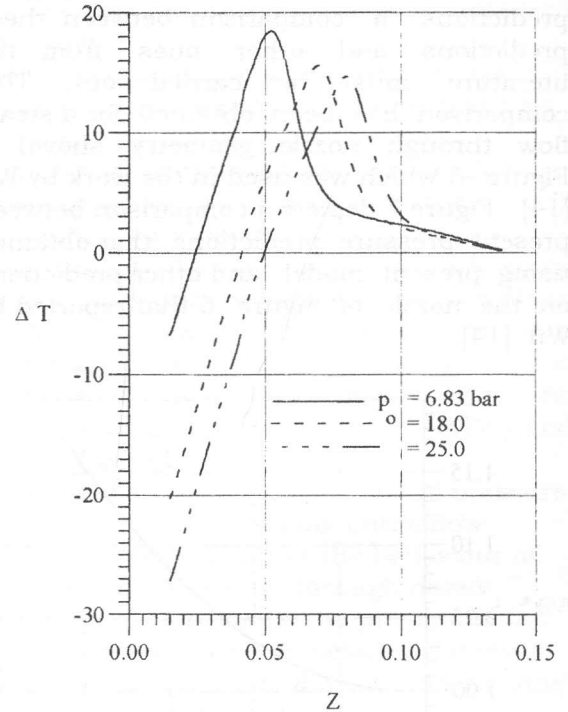
**Figure 4** Effect of changing the coefficient ( $\beta$ ) on the flow characteristics at constant values of  $p_0 = 6.83$  bar,  $\alpha_c = 1.0$  &  $\Delta T_1 = 3$  K



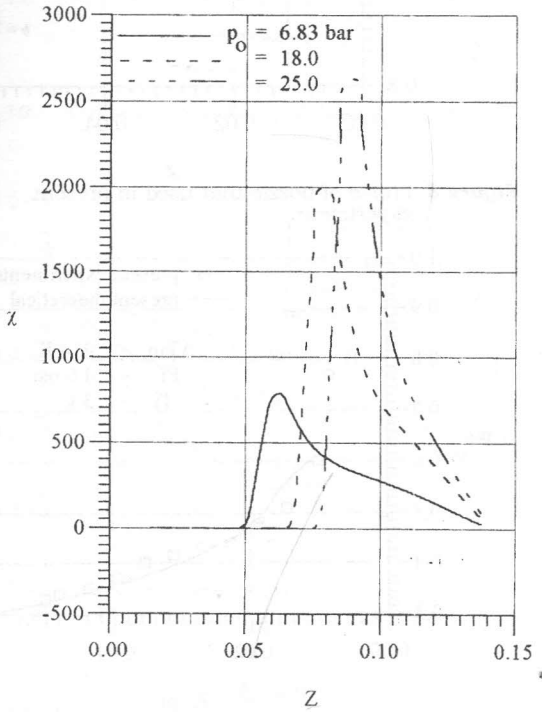
# Investigation of Unsteady Two-Phase Flow of Wet Steam Through Nozzles



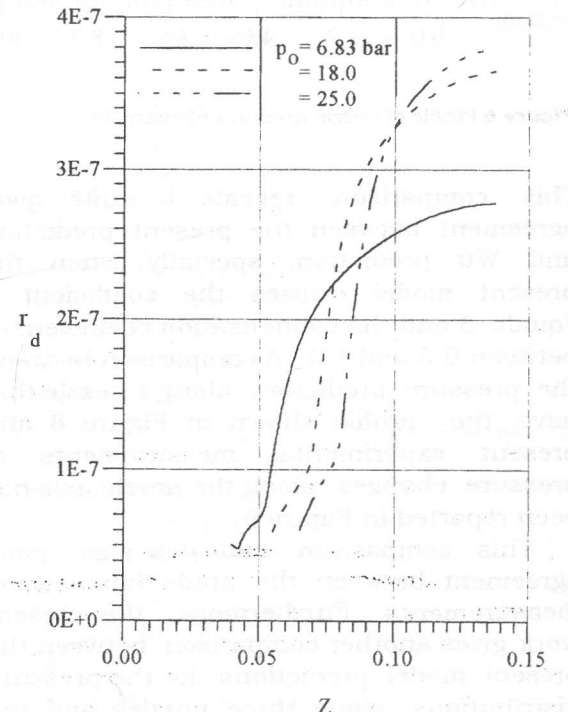
a- pressure variation along nozzle axis.



b- vapour subcooling along nozzle axis.



c- phase conversion rate along nozzle axis.



d- mean droplet size along nozzle axis.

**Figure 5** Effect of changing the initial pressure on the flow characteristics at constant values of  $\alpha_c=1.0$ ,  $\beta=1.0$  &  $\Delta T_1=3$  K.

In order to confirm the present predictions, a comparison between these predictions and other ones from the literature must be carried out. This comparison has been obtained for a steam flow through nozzle geometry shown in Figure 6 which was used in the work by Wu [14]. Figure 7 depicts a comparison between present pressure predictions that obtained using present model and other predictions on the nozzle of Figure 6 that reported by Wu. [14].

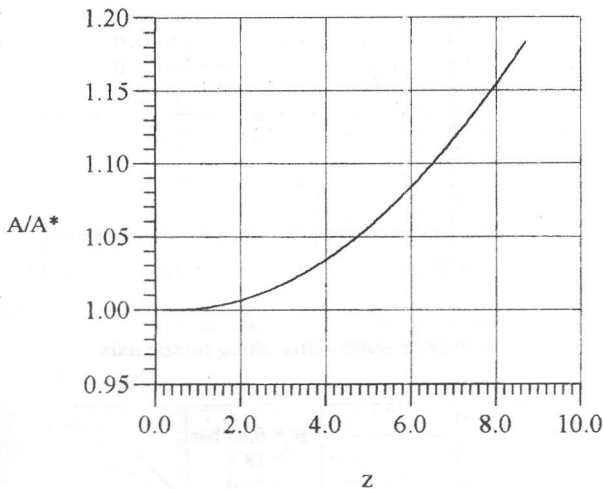


Figure 6 Profile of nozzle used in Reference 14.

This comparison reveals a quite good agreement between the present prediction and Wu prediction, specially when the present model utilizes the coefficient  $\beta$  equals 3 and the condensation coefficient  $\alpha_c$  between 0.5 and 1.0. A comparison between the pressure prediction along a nozzle that have the profile shown in Figure 8 and present experimental measurements of pressure changes along the nozzle axis has been reported in Figure 9.

This comparison indicates also good agreement between the prediction and the measurements. Furthermore, the present work gives another comparison between the present model predictions for the pressure distributions along three nozzles and the measured values of these distributions that have been reported by Bakhtar [15].

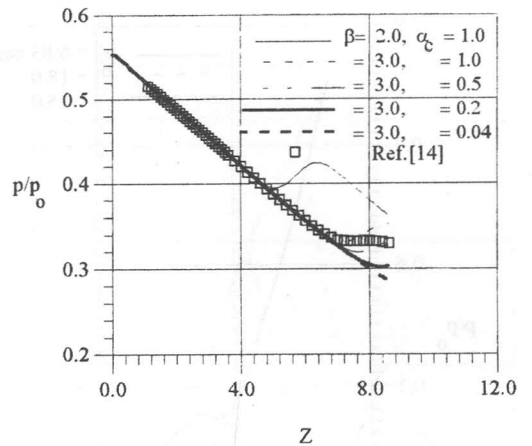


Figure 7 A comparison between present predictions and Wu [14] predictions.

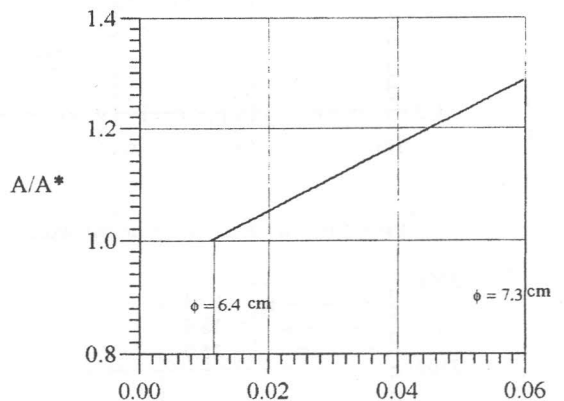


Figure 8 Profile of nozzle that used in present experiment.

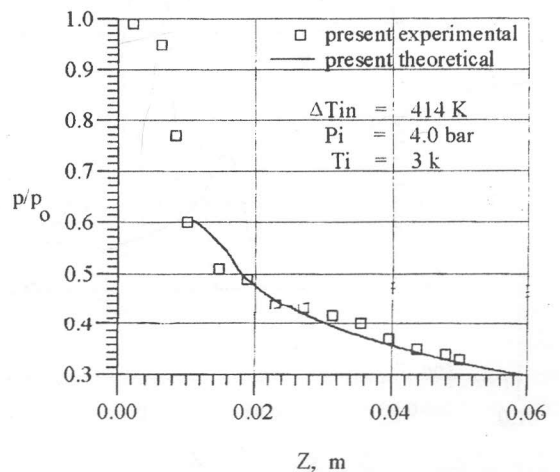


Figure 9 A comparison between present predictions and present experiments of pressure variation along nozzle (3).

Profiles of these nozzles are illustrated in Figure 10. It can be seen in Figure 11 that the agreement between the present predictions and Bakhtar's measured pressure distributions of steam flows through these nozzles is good except in the case of nozzle L. The disagreement between present predictions and experimental pressure distributions can be attributed to the errors in measuring the inlet temperature of steam ahead the nozzle entrance as discussed by Bakhtar [15].

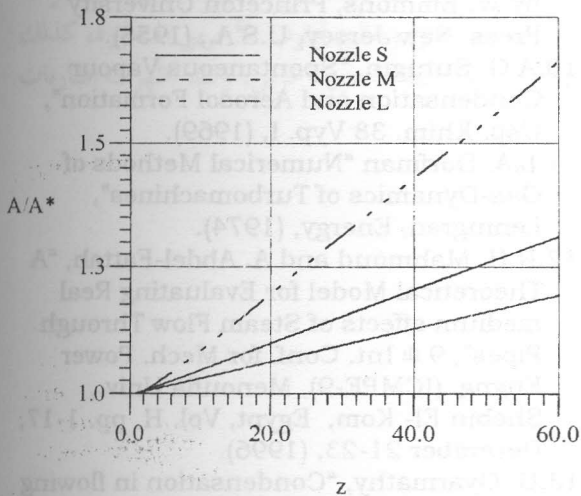


Figure 10 Profiles of nozzles S, M & L from Reference 15

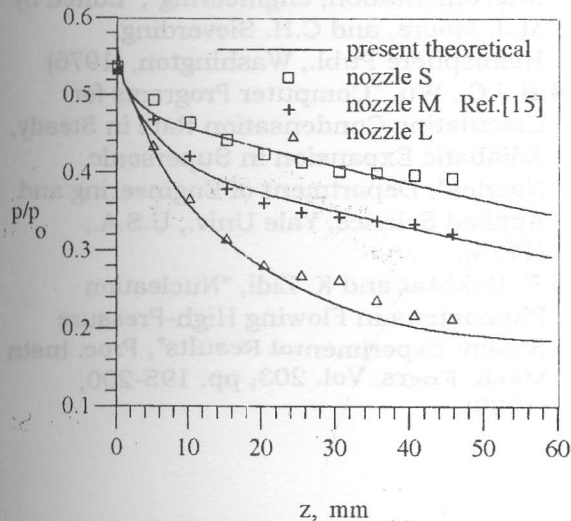


Figure 11 Comparison between present predictions and measured values of pressure variation along nozzles by Reference 5.

### CONCLUSIONS

The present results may be summarized as follows:

- 1- Increasing the condensation coefficient only in the theoretical model suppresses both the subcooling ( $\Delta T$ ) and the rate of phase conversion, while rises the flow pressure and mean radius of the condensed water droplets.
- 2- Increasing the coefficient  $\beta$ , while keeping the other parameters constant, results in the damping of the pressure gradient along the nozzle passage and consequently increasing the condensation parameters, i.e., ( $\Delta T$ );  $\chi$  and  $r_d$ , of wet steam flow.
- 3- Increasing the steam flow initial pressure, as a sample of changing initial flow parameters, can affect the behaviour of steam condensation through nozzle.
- 4- Comparison between the present model predictions, based on selected values for the coefficients  $\alpha_c$  and  $\beta$ , and predictions of other investigators and present measurements showed good agreement.

### NOMENCLATURE

- A: nozzle area;  $m^2$
- B: compressibility;
- c: velocity;  $m.s^{-1}$
- D: simplifying symbol;
- e: internal energy;  $kJ.kg^{-1}$
- i: enthalpy;  $kJ.kg^{-1}$
- J: nucleation rate;  $s^{-1}$
- k: Boltzman constant;  $J.K^{-1}$
- L: nozzle length; m
- m: droplet mass; kg
- $m_o$ : molecular weight;  $mol.kg^{-1}$
- N: non-normalizing density distribution of droplet;
- p: pressure; bar
- $r_d$ : droplet radius; m
- $r_c$ : critical dimension of nucleus; m
- R: gas constant;  $kJ.kg^{-1}.K^{-1}$
- S: entropy;  $kJ.kg^{-1}.K^{-1}$
- t: time; s
- T: absolute temperature;  $K^{-1}$
- $v_m$ : volume per one molecule in a condensed phase;  $m^3.mol^{-1}$
- u: simplifying symbol;
- z: distance along nozzle axis; m

- $\alpha_c$ : condensation coefficient;  
 $\beta$ : correction factor for nucleation work;  
 $\gamma$ : specific heat ratio;  
 $\sigma$ : surface tension coefficient;  $N.m^{-1}$   
 $\rho$ : density;  $kg.m^{-3}$   
 $\mu$ : Gibbs function;  $kJ.kg^{-1}$   
 $\zeta$ : latent heat of evaporation;  $kJ.kg^{-1}$   
 $\chi$ : phase conversion rate;  $kg.m^{-3}.s^{-1}$   
 $\Delta w$ : nucleation work;  $N.m$

**Subscripts**

- 1: vapour phase;  
 2: water phase;  
 ∞: critical;  
 c: condensed;  
 d: droplet;  
 0: stagnation;  
 s: saturation;

**Superscripts**

- l: left;  
 r: right;

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## فحص السريان ثنائي الطور الغير مستقر للبخار الرطب خلال الأبواق

مفرح حمادة حامد

قسم هندسة القوى الميكانيكية - جامعة المنوفية

### ملخص البحث

تصف هذه الورقة نموذجاً نظرياً لحل السريان الأحادي البعد غير المستقر للبخار الرطب بالتكثف التلقائي (اللحظي) خلال أبواق فوق صوتيه، بأخذ النموذج في الاعتبار إدخال تأثير المعامل  $\beta$  وهو معامل تصحيح لشغل تكوين الأنوية في أس معادلة معدل تكون الأنوية، كذلك بأخذ النموذج الرياضي في الاعتبار تأثير معامل لتكثيف  $\alpha_c$ . كما تعقد الورقة مقارنات بين التنبؤات المأخوذة من النموذج المقترح هنا ونتائج القياسات العملية لكل من تجارب البحث الحالي ونتائج تجارب الآخرين المنشورة، كذلك فان الورقة تقدم مقارنات أخرى بين النتائج النظرية للنموذج المقترح ونتائج نظرية سابقة لباحثين آخرين، ولقد أظهرت المقارنات توافقاً مقبولاً.