

FREE CONVECTION IN INCLINED AIR LAYERS HEATED FROM ABOVE

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ABSTRACT

An experimental investigation of steady state natural convection heat transfer was carried out in finite rectangular air layers heated from above. Two different aspect ratios, namely $A=20$ and 80 , and perfectly conducting boundary conditions on the end walls were used. The angle of inclination was varied from $\dot{U} = 0$ (heated from below) to $\dot{U} = 180$ deg (heated from above). A total of 226 test points were taken for heat transfer measurements in air layers heated from above at four different orientations in the range $120 \mu \dot{U} \mu 180$ deg for Rayleigh numbers between 10^2 and 2×10^6 . Additional test points have been carried out to show the effect of the angle of tilt in the range $0 \mu \dot{U} \mu 180$ deg on the average Nusselt number for fixed values of the Rayleigh number. Local measurements of the Nusselt number over discrete portions of the air layer are reported to show the Nusselt number distribution over different flow regimes.

1. INTRODUCTION

The problem of steady state two-dimensional natural convection in an enclosed tilted rectangular cavity heated from below has been the subject of several numerical, analytical and experimental studies. A comprehensive review is given by Catton [1]. In addition, the problem of increasing heat transfer by free convection in a liquid or gas-filled cavity by heating from above is of great interest. However, this case of tilted layers heated from above has received little attention and a serious lack of experimental data in this area is noticed. Figure (1) shows a sketch of a tilted rectangular air layer. It consists of two parallel flat plates with one surface heated at a constant temperature of T_h and the other one cooled at a constant temperature of T_c . The cavity is closed at the ends by surrounding a solid strip of thickness B and thermal conductivity K_o . The cavity aspect ratio is defined as the ratio of the height H to the plate spacing L ($A = H/L$). The thermal boundary conditions on the end walls can be defined through the ratio of the end walls and fluid thermal conductivities K_o/K and the ratio L/B . Koutsoheras and Charters [2] studied the effect of the end walls thermal boundary conditions on the natural convection across air cavities. Two extremes are known as limits for the boundary conditions. These are the perfectly insulating or zero heat flux (ZHF) and perfectly conducting or linear

temperature profile (LTP) end walls. The two dimensional numerical study of Koutsoheras and Charters [2] covered the range $1 \mu L/B \mu 10$ and $0 \mu K_o/K \mu \infty$ for small aspect ratios $1/3 \mu A \mu 3$. They reported heat transfer results only for $A=1$ and $0 \mu \dot{U} \mu 90$ deg (heated from below).

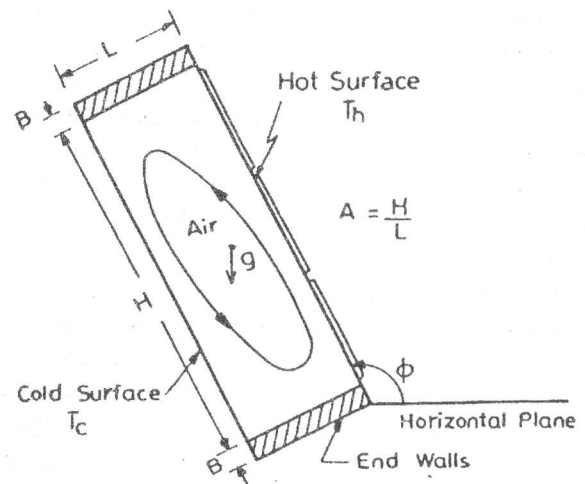


Figure 1. A sketch of the problem.

Catton et al [3] used the Galerkin method to solve the two dimensional steady flow of infinite Prandtl number in tilted rectangular cavities. They reported results in

the range 0.2μ A μ 20 and 60μ $\dot{U} \mu$ 165 deg for both adiabatic and perfectly conducting boundary conditions on the border strips. They found that thermal instabilities associated with regions of adverse temperature gradient (due to the presence of perfectly conducting end walls) should be possible even in the case of top heating which is known as convectively stable regime. These effects would be more pronounced for the case of finite Prandtl number. An experimental study was performed by Arnold et al [4] using high Prandtl number fluids (silicon oils and water) in layers of aspect ratios $A = 1, 3, 6,$ and 12 . The angle of tilt was varied between $\dot{U} = 0$ (heated from below) to $\dot{U} = 180$ deg (heated from above) and measurements were taken for Rayleigh numbers between 10^3 and 10^6 . They derived the following scaling law for angles of inclination from $\dot{U} = 90$ deg (vertical layers) to $\dot{U} = 180$ deg (heated from above)

$$Nu(\dot{U}) = 1 + [Nu(\dot{U} = 90^\circ) - 1] \cdot \sin \phi \quad (1)$$

An experimental and numerical study was given by Ozoe et al [5] for high Prandtl number ($Pr = 10$) in an inclined square cavity. The case for adiabatic boundary conditions was tested in a limited range of Rayleigh numbers between 2000 and 8000 for layers heated from below $0 \leq \phi \leq 90$ deg. A local maximum in the average Nusselt number was found to occur at about 50 degrees of inclination. This study was extended by Ozoe et al [6] for higher values of the aspect ratio $A = 1, 2, 3$ and 4 , and the angle of inclination was varied between 0 and 180 deg. Their experimental results using silicon oils ($Pr = 4045$) were in good agreement with the numerical predictions.

The only previous comprehensive study for inclined air layers heated from above was given in the Housing Research Paper No. 32 [7]. This work was done at the National Bureau of Standards, U.S.A. using air layers of aspect ratios in the range $18 \leq A \leq 96$. The paper presented the measurements of heat transfer for air spaces of various emissivities and thicknesses. A total of 146 test points were taken for air spaces at five different orientations in the range $0 \leq \phi \leq 180$ deg using an apparatus of the guarded hot box type. The experimental results were given as plots of the value hL against ΔTL^3 for fixed values of the angle of

inclination. Tabor [8] reduced the results given in Ref. [7] to the usual non-dimensional groups of Nusselt against Grashof numbers. The purpose of the present work is to provide a definitive study and heat transfer results for natural convection in tilted air layers heated from above.

2. TEST APPARATUS

The present investigation was carried out on the same test apparatus built by the author and fully explained in a previous study [9]. As shown in Figure (2), it consists of two parallel flat copper plates each measured 635 by 635 by 12.7 mm thickness in overall dimensions. In the present experiments, the heat flux across the air cavity was measured over the full length H of the hot plate. This was done by inserting three electrically heated heater plates into three recesses along the vertical centerline of the hot plate. Each heater plate measured 200 by 200 by 3.1 mm thickness in overall dimensions. A heat flux meter was inserted below each heater plate. Thus an average value of the heat flux was measured for each third of the plate height. To maintain isothermal surfaces on the copper plates, each of the hot and cold plates was connected to a constant temperature water bath with its thermostat set at fixed but different temperature. The hot or cold water was circulated through tubes soldered to the back of each copper plate. A thermopile consisting of six copper - constantan thermocouples embedded in each plate was used to measure the temperature difference ΔT between the two copper plates. Perfectly conducting boundary conditions on the end walls were established by surrounding the air layer at the four sides by a copper sheet of 0.50 mm thickness.

The Rayleigh number was varied by varying the air pressure inside the cavity while the spacing L and the temperature difference ΔT were kept unchanged. This method was used to separate the effect of the Rayleigh number on Nusselt number from any other effects due to the variation in aspect ratio or thermal properties of air. Therefore, the two plates were enclosed in a pressure vessel where the pressure can be varied from 100 Pa to 0.7 MPa. The pressure vessel can be rotated around a horizontal axis to give any required angle of tilt.

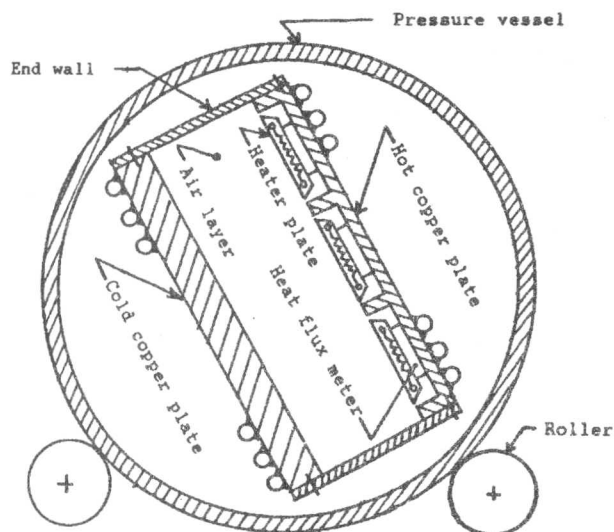


Figure 2. A sketch of test apparatus.

3. RESULTS AND DISCUSSION

In the present study, heat transfer measurements were taken for inclined rectangular air layers heated from above with two different fixed values of the aspect ratio $A = 20$ and 80 . Perfectly conducting boundary conditions were used on the end walls. Figure (3) shows the data for both aspect ratios for air layers tilted at 120 and 135 degrees from the horizontal. For $\phi = 120$ deg, it is clear that conduction regime prevailed up to $Ra = 3000$ and then the Nusselt number started to deviate from the value of pure conduction ($Nu = 1$) till the data finally took a one third slope at $Ra \geq 3 \times 10^4$ indicating a change to the turbulent flow regime. Increasing the aspect ratio from 20 to 80 resulted in a reduction in the Nusselt number. For $\phi = 135$ deg, the same general behaviour was obtained with departure from pure conduction at a slightly higher Rayleigh number for the higher aspect ratio. The experimental data from Ref.[7] are plotted on the same figure for $\phi = 135$ deg. It should be noted that the Rayleigh number for the data from Ref. [7] was increased by increasing the plate spacing L ; i.e. decreasing the aspect ratio. Thus no aspect ratio effect was detected in their data. The dashed line

representing the data from Ref. [7] for $18 \leq A \leq 96$ follows the present data for high aspect ratio ($A=80$) at low Ra and gradually moves to follow the present data for low aspect ratio ($A = 20$) for the higher range of Ra . The departure from the pure conduction regime occurred exactly at the same Rayleigh number and the turbulent flow regime occurred at $Ra \geq 8 \times 10^4$.

Figure (4) shows the data from the present study for $A = 20$ and 80 at $\phi = 150$ deg and $\phi = 180$ deg. For $\phi = 150$ deg, again the flow changed from pure conduction at $Ra \approx 4000$ and the slope of the data increased till it reached the one third slope at $Ra \geq 2 \times 10^5$. This indicates that as ϕ was increased (getting closer to horizontal layer heated from above), the change to the turbulent flow occurred at higher values of Ra . For $\phi = 180$ deg (horizontal layer heated from above), the conduction regime prevailed up to $Ra = 10^4$. However, convection started to contribute to the heat transfer across the air layer as was expected by Catton et al [3] due to the presence of perfectly conducting end walls. The dashed line representing the data from Ref. [7] follows very close the present data.

Additional experiments have been carried out to explain the effect of angle of tilt on the average Nusselt number for fixed values of the Rayleigh number. The experimental results are plotted in Figure (5) for $A=20$ and the tilt angle was varied from 0 (heated from below) to 180 deg (heated from above). It is clear that the average Nusselt number decreased monotonically as the angle of tilt was increased from 0 to 180 deg. The scaling law derived by Arnold et al [4] and given by equation (1) is drawn in Fig.5 in its range of applicability ($90 \leq \phi \leq 180$ deg). It is seen that the present data approximately follow the same scaling law especially at high Rayleigh numbers with a maximum deviation of less than 10% . Although the scaling law for $\phi = 180$ deg assumes totally pure conduction, the present data and those of Ref. [7] show a real contribution of the convection due to the perfectly conducting boundary conditions on the end walls. For tilted layers heated from above, the average Nusselt number is considerably greater than that for pure conduction.

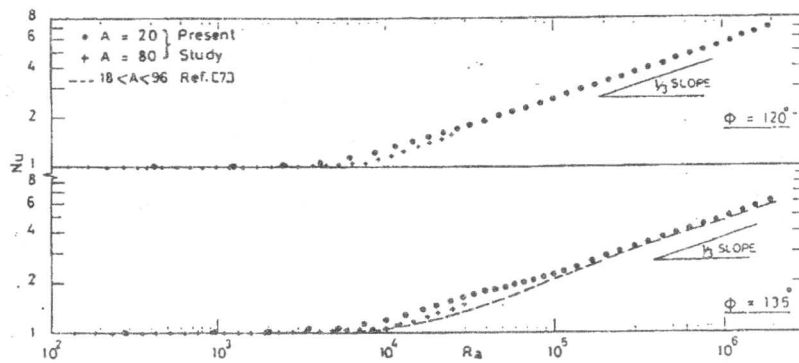


Figure 3. Heat transfer measurements for $\phi = 120$ and 135 degrees.

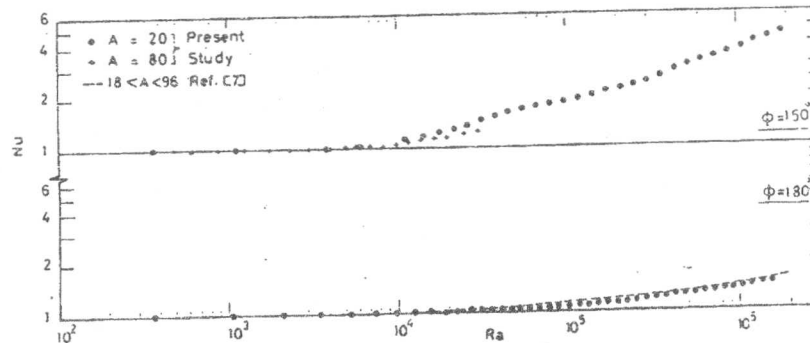


Figure 4. Heat transfer measurements for $\phi = 150$ and 180 degrees.

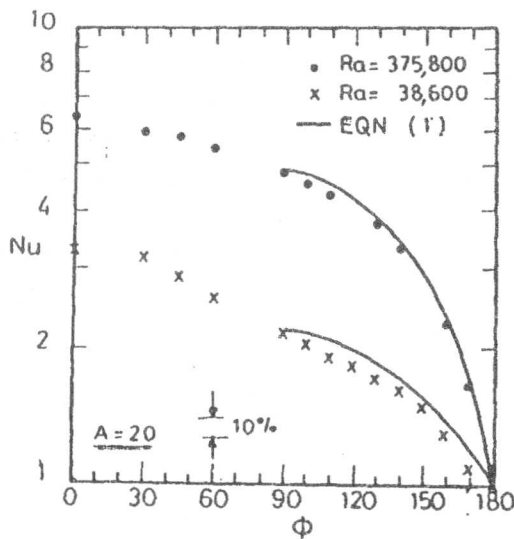


Figure 5. Effect of tilt angle on Nu.

To the author knowledge, no previous measurements were published for local Nusselt numbers in air layers heated from above. The distribution of Nusselt number along the height of the air layer is seen in Figure (6) for $A = 20$ and $\phi = 120$ deg. The data represent the average Nusselt number on the lower, middle, and

upper third of the hot plate. In the conduction regime, $Ra < 1000$, the three values were equal to unity. As Ra was increased, the average Nusselt number over the lower third of the hot plate increased very quickly and finally approached $1/3$ slope at $Ra \geq 4 \times 10^5$. In the middle third of the layer, the average Nusselt number slowly increased and reached the same $1/3$ slope at $Ra \geq 4 \times 10^5$. In the upper third of the hot plate, the average Nu continuously dropped below unity as Ra was increased till it reached a minimum value of 0.77 at $Ra = 1.45 \times 10^4$. A further increase in Ra caused the average Nu on the upper third to increase till it approached the same $1/3$ slope at $Ra \geq 4 \times 10^5$. The average Nusselt number over the entire hot plate is plotted on the same figure as a solid line. It is clear that the average Nusselt number on the central portion of the hot plate underestimates the average Nusselt number on the entire plate till Ra reaches a high value of 4×10^5 . This indicates that for air layers heated from above, measurements averaged over the central portion do not exactly represent measurements averaged over the entire plate unless the Rayleigh number is very high ($\geq 4 \times 10^5$).

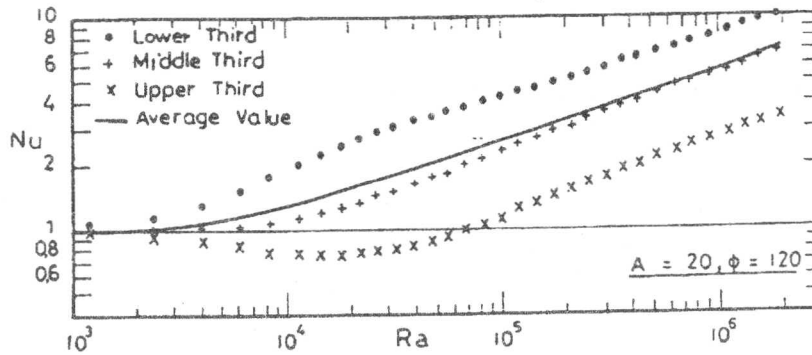
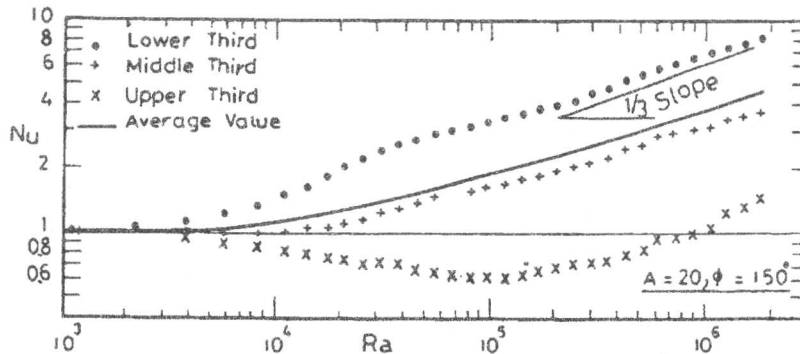
Figure 6. Nusselt number distributions for $\phi = 120$ degrees.Figure 7. Nusselt number distributions for $\phi = 150$ degrees.

Figure (7) shows the distribution of the Nusselt number along the hot plate for $A = 20$ and $\phi = 150$ deg. The same behaviour is repeated where the average Nu over the lower third quickly increased and then came back to the $1/3$ slope at $Ra \approx 3 \times 10^4$. The data from the middle third of the hot plate fell below the average Nu for the entire plate. This continued for all values of Ra beyond the pure conduction regime. The average value of Nu for the upper third continuously dropped to a new lower minimum value of 0.62 at $Ra \approx 10^5$. Turning the air layer from $\phi = 120$ deg to $\phi = 150$ deg has the effect of damping the flow inside the layer for a fixed value of Rayleigh number. For $Ra > 10^5$, the average Nu for the upper third started to increase as Ra was increased.

ACKNOWLEDGMENT

This study was carried out in the Heat Transfer Laboratory of the Mechanical Engineering Department, University of Waterloo, Canada. The advice of Prof. K.G.T. Hollands is gratefully acknowledged.

Nomenclature

- A aspect ratio ($A = H/L$)
- B thickness of end walls
- g gravitational acceleration
- h average heat transfer coefficient between isothermal plates
- H plate height
- K thermal conductivity of air
- K_o thermal conductivity of end walls
- L plate spacing
- Nu average Nusselt number, $Nu = hL/K$
- Pr Prandtl number, $Pr = \nu/\alpha$
- Ra Rayleigh number, $Ra = L^3 \beta g \Delta T / \nu \alpha$
- T_c temperature of cold plate
- T_h temperature of hot plate

Greek symbols

- α thermal diffusivity of air
- β volumetric thermal expansion coefficient of air
- ΔT plate temperature difference, $\Delta T = T_h - T_c$
- ϕ angle of tilt from horizontal
- ν kinematic viscosity of air

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